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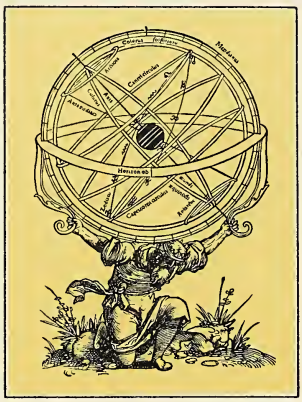

PROSPECTUS

OF A

COURSE OF LECTURES

ON SOME OF THE PRACTICAL PARTS

OF THE

MATHEMATICS,

VIZ.

PART FIRST.	*PART SECOND.*
ASTRONOMY,	GUNNERY,
GEOGRAPHY,	AND
NAVIGATION.	FORTIFICATION.

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PROSPECTUS

OF A

COURSE OF LECTURES, &c.

[*Edinburgh College, October* 18. 1793.]

ASTRONOMY.

I.

GENERAL view of the Phœnomena of the Heavens.—Apparent Motion of the fixed Stars, of the Sun, Moon, Planets, Satellites of the Planets, Comets.—To have a more accurate knowledge of theſe, the Doctrine of the Sphere muſt be explained.—Definitions.—

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NAVIGATION.

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Note. The diviſions in this Proſpectus do not refer to the Number of the Lectures, but of the Heads under which the Lectures are arranged.